

14. We make use of Eq. 4-16.

(a) The acceleration as a function of time is

$$\vec{a} = \frac{d\vec{v}}{dt} = \frac{d}{dt} \left( (6.0t - 4.0t^2)\hat{i} + 8.0\hat{j} \right) = (6.0 - 8.0t)\hat{i}$$

in SI units. Specifically, we find the acceleration vector at  $t = 3.0$  s to be  $(6.0 - 8.0(3.0))\hat{i} = (-18 \text{ m/s}^2)\hat{i}$ .

(b) The equation is  $\vec{a} = (6.0 - 8.0t)\hat{i} = 0$ ; we find  $t = 0.75$  s.

(c) Since the  $y$  component of the velocity,  $v_y = 8.0$  m/s, is never zero, the velocity cannot vanish.

(d) Since speed is the magnitude of the velocity, we have

$$v = |\vec{v}| = \sqrt{(6.0t - 4.0t^2)^2 + (8.0)^2} = 10$$

in SI units (m/s). We solve for  $t$  as follows:

$$\text{squaring } (6.0t - 4.0t^2)^2 + 64 = 100$$

$$\text{rearranging } (6.0t - 4.0t^2)^2 = 36$$

$$\text{taking square root } 6.0t - 4.0t^2 = \pm 6.0$$

$$\text{rearranging } 4.0t^2 - 6.0t \pm 6.0 = 0$$

$$\text{using quadratic formula } t = \frac{6.0 \pm \sqrt{36 - 4(4.0)(\pm 6.0)}}{2(4.0)}$$

where the requirement of a real positive result leads to the unique answer:  $t = 2.2$  s.